

# Properties of SVM

- Flexibility in choosing a similarity function
- **Sparseness** of solution when dealing with large data sets
  - only support vectors are used to specify the separating hyperplane
- Ability to **handle large feature spaces**
  - complexity does not depend on the dimensionality of the feature space
- Overfitting can be controlled by soft margin approach
- **Nice math property**: a simple convex optimization problem which is guaranteed to converge to a single global solution
- Feature Selection

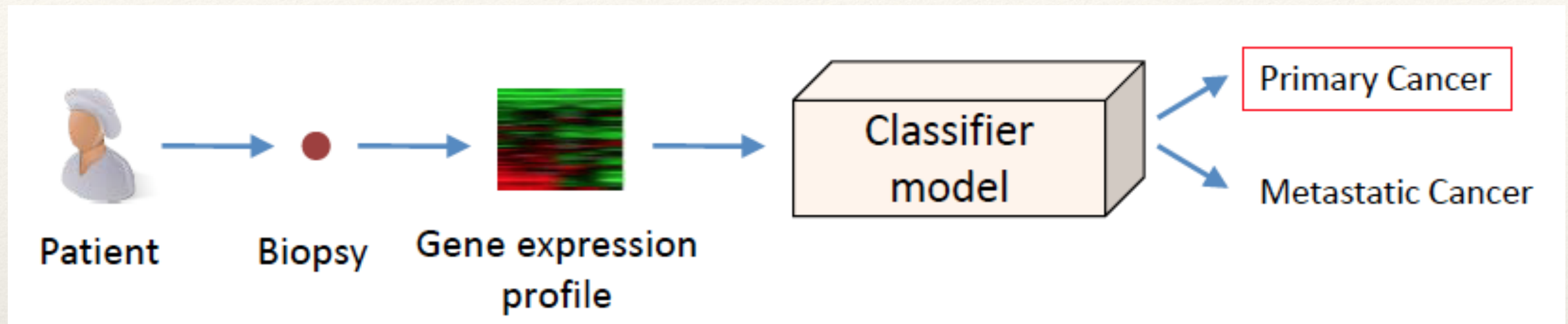


# SVM Applications

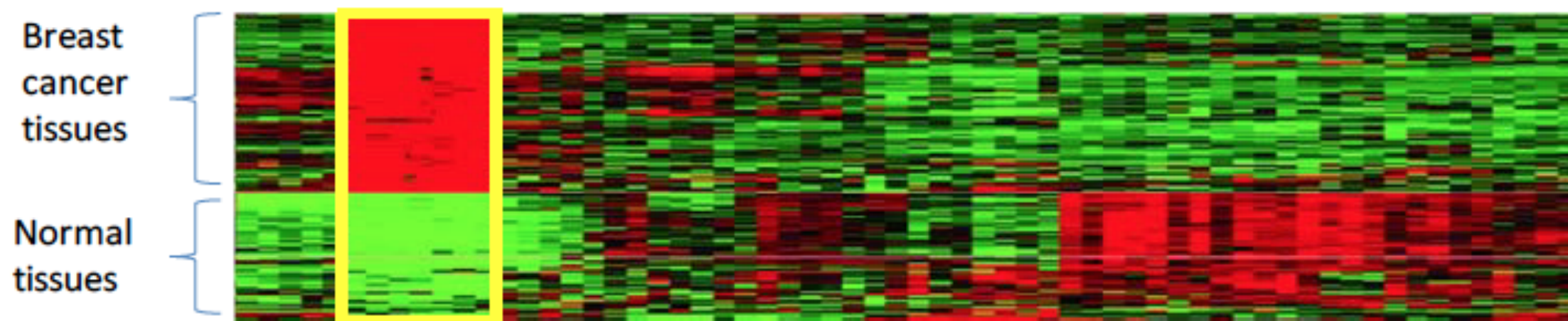
- SVM has been used successfully in many real-world problems
  - text (and hypertext) categorization
  - image classification
  - bioinformatics (Protein classification, Cancer classification)
  - hand-written character recognition



# Application 1: Cancer Classification



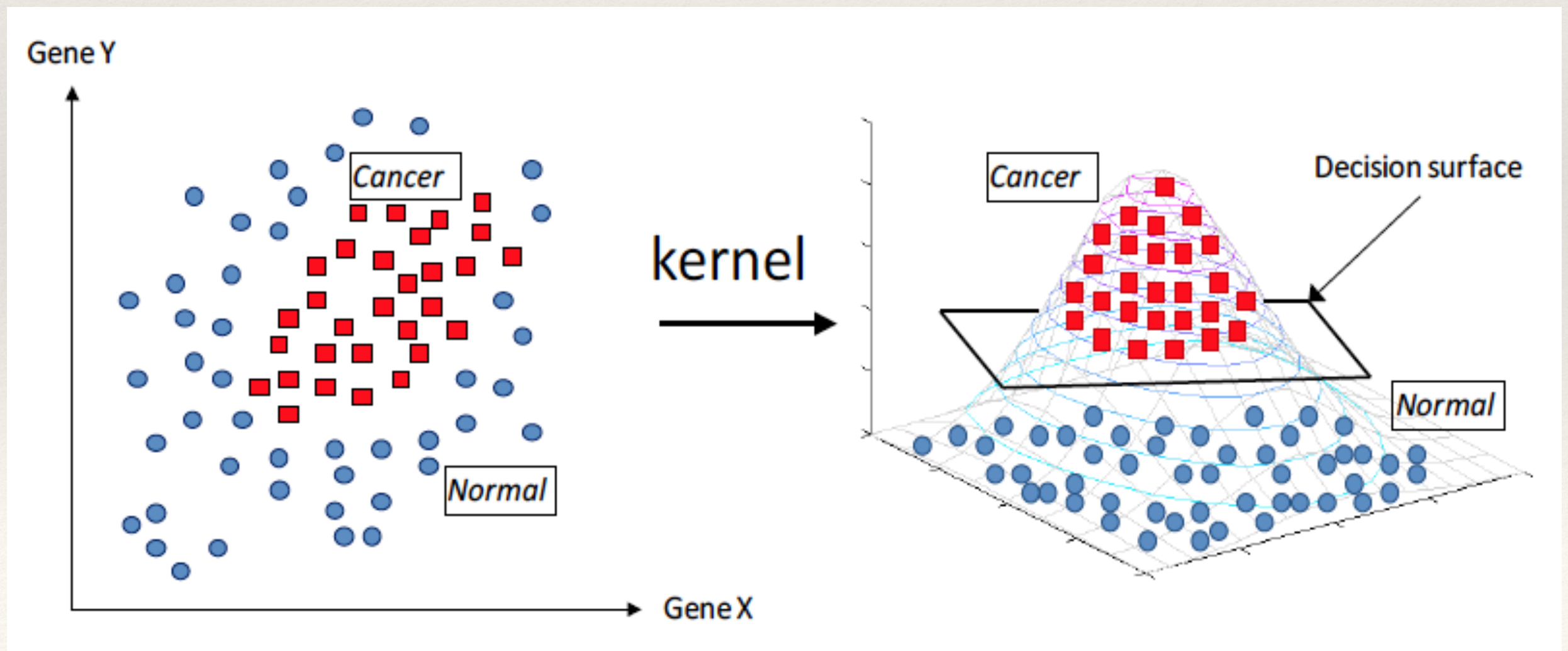
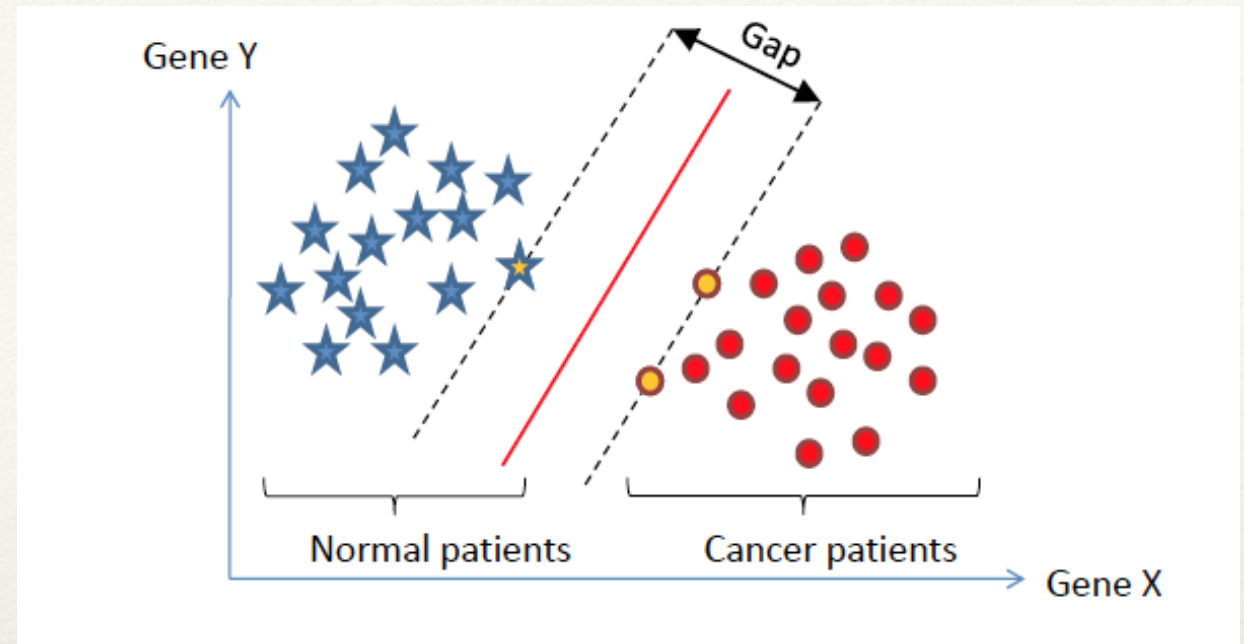
- E.g., find the most compact panel of breast cancer biomarkers from microarray gene expression data for 20,000 genes:



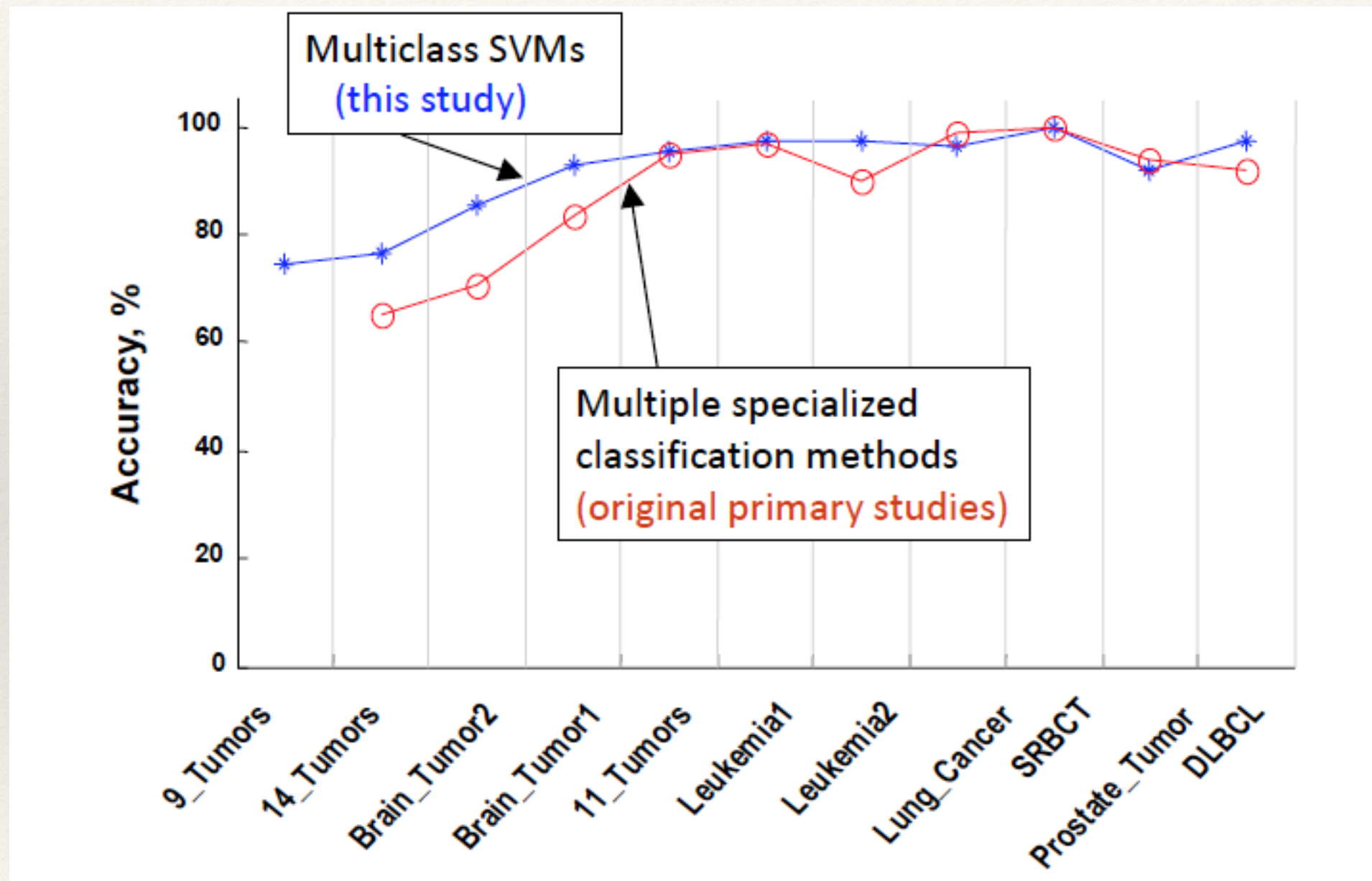


# Application 1: Cancer Classification

Linear Versus Non-linear SVMs



# Application 1: Cancer Classification





# Weakness of SVM

- **It is sensitive to noise**

- A relatively small number of mislabeled examples can dramatically decrease the performance

- **It only considers two classes**

- how to do multi-class classification with SVM?

- Answer:

- 1) with output  $m$ , learn  $m$  SVM's

- SVM 1 learns "Output==1" vs "Output != 1"
- SVM 2 learns "Output==2" vs "Output != 2"
- :
- SVM  $m$  learns "Output== $m$ " vs "Output !=  $m$ "

- 2) To predict the output for a new input, just predict with each SVM and find out which one puts the prediction the furthest into the positive region.



# Application 2: Text Categorization

- Task: The classification of natural text (or hypertext) documents into a fixed number of predefined categories based on their content.
  - email filtering, web searching, sorting documents by topic, etc..
- A document can be assigned to more than one category, so this can be viewed as a series of binary classification problems, one for each category.



# Application 2: Text Categorization

IR's vector space model (aka bag-of-words representation)

- A doc is represented by a vector indexed by a pre-fixed set or dictionary of terms
- Values of an entry can be binary or weights

$$\phi_i(x) = \frac{\text{tf}_i \log(\text{idf}_i)}{\kappa},$$

- Doc  $\mathbf{x} \Rightarrow \phi(\mathbf{x})$



# Application 2: Text Categorization

- The distance between two documents is  $\langle \phi(x) \phi(z) \rangle$
- $K(x,z) = \langle \phi(x) \phi(z) \rangle$  is a valid kernel, SVM can be used with  $K(x,z)$  for discrimination.
- Why SVM?
  - High dimensional input space
  - Few irrelevant features (dense concept)
  - Sparse document vectors (sparse instances)
  - Text categorization problems are linearly separable



# Application 2: Text Categorization

	Bayes	Rocchio	C4.5	k-NN	SVM (poly) degree $d =$					SVM (rbf) width $\gamma =$					
					1	2	3	4	5	0.6	0.8	1.0	1.2		
earn	95.9	96.1	96.1	97.3	98.2	98.4	<b>98.5</b>	98.4	98.3	<b>98.5</b>	98.5	98.4	98.3		
acq	91.5	92.1	85.3	92.0	92.6	94.6	<b>95.2</b>	95.2	95.3	95.0	95.3	95.3	<b>95.4</b>		
money-fx	62.9	67.6	69.4	78.2	66.9	72.5	75.4	74.9	<b>76.2</b>	74.0	75.4	<b>76.3</b>	75.9		
grain	72.5	79.5	89.1	82.2	91.3	93.1	<b>92.4</b>	91.3	89.9	<b>93.1</b>	91.9	91.9	90.6		
crude	81.0	81.5	75.5	85.7	86.0	87.3	88.6	<b>88.9</b>	87.8	<b>88.9</b>	89.0	88.9	88.2		
trade	50.0	77.4	59.2	77.4	69.2	75.5	76.6	77.3	<b>77.1</b>	76.9	78.0	<b>77.8</b>	76.8		
interest	58.0	72.5	49.1	74.0	69.8	63.3	67.9	73.1	<b>76.2</b>	74.4	75.0	<b>76.2</b>	76.1		
ship	78.7	83.1	80.9	79.2	82.0	85.4	86.0	<b>86.5</b>	86.0	<b>85.4</b>	86.5	87.6	87.1		
wheat	60.6	79.4	85.5	76.6	83.1	84.5	85.2	<b>85.9</b>	83.8	<b>85.2</b>	85.9	85.9	85.9		
corn	47.3	62.2	87.7	77.9	86.0	86.5	85.3	<b>85.7</b>	83.9	<b>85.1</b>	85.7	85.7	84.5		
microavg.	<b>72.0</b>	<b>79.9</b>	<b>79.4</b>	<b>82.3</b>	84.2	85.1	85.9	86.2	85.9	combined: <b>86.0</b>		86.4	86.5	86.3	86.2
										combined: <b>86.4</b>					



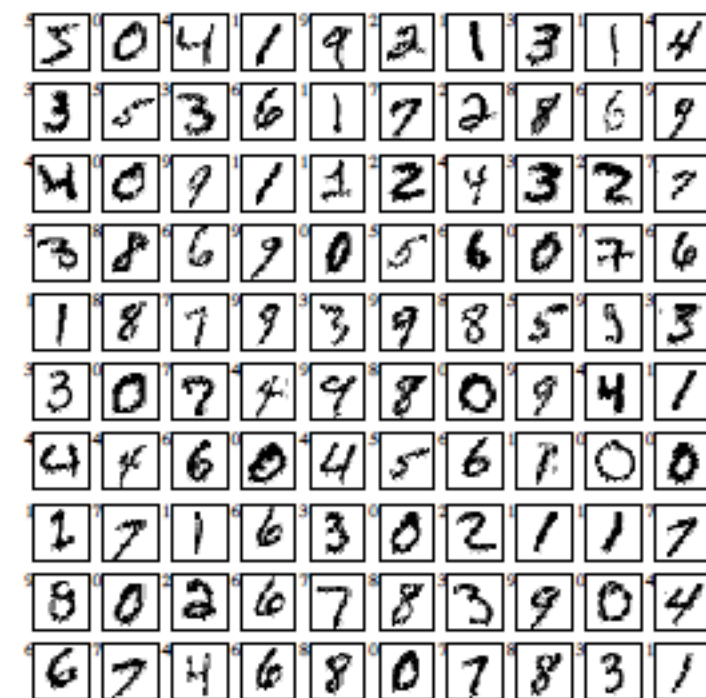
# Application 3: Handwriting Recognition

For example MNIST hand-writing recognition.

60,000 training examples, 10000 test examples, 28x28.

Linear SVM has around 8.5% test error.

Polynomial SVM has around 1% test error.



## SVMs : full MNIST results

Classifier	Test Error
linear	8.4%
3-nearest-neighbor	2.4%
RBF-SVM	1.4 %



# Some Considerations

- Choice of kernel
  - Gaussian or polynomial kernel is default
  - if ineffective, more elaborate kernels are needed
  - domain experts can give assistance in formulating appropriate similarity measures
- Choice of kernel parameters
  - e.g.  $\sigma$  in Gaussian kernel
  - $\sigma$  is the distance between closest points with different classifications
  - In the absence of reliable criteria, applications rely on the use of a validation set or cross-validation to set such parameters.
- Optimization criterion – Hard margin v.s. Soft margin
  - a lengthy series of experiments in which various parameters are tested



# Software

## **30 SVMs : software**

Lots of SVM software:

- LibSVM (C++)
- SVMLight (C)

As well as complete machine learning toolboxes that include SVMs:

- Torch (C++)
- Spider (Matlab)
- Weka (Java)

All available through [www.kernel-machines.org](http://www.kernel-machines.org).